

Hadron-to-muon branching ratio for e⁻e⁺ annihilation:

$$R = \frac{\sigma(e^-e^+ \rightarrow \text{hadrons})}{\sigma(e^-e^+ \rightarrow \mu^-\mu^+)} \approx \frac{\text{Feynman Diagram (Hadrons)}}{\text{Feynman Diagram (Muons)}} \approx \frac{\sum_i A Q_i^2}{A Q_\mu^2}$$

The e⁻e⁺ annihilation will produce a particle-antiparticle pair of either leptons or quarks. The probability or cross-section for each type of pair can be computed using QED (with the dominant contribution coming from the lowest order Feynman diagrams shown above). In general, these cross-sections σ are a function of total collision energy E , however, for sufficiently large E (well above the production threshold $2M_i c^2$) $\sigma_i \approx A Q_i^2$. Thus, the ratio R provides a measure of the number of different types of quarks. The original quark model predicted 3 quarks with charges $2/3$, $-1/3$, and $-1/3$ which should give $R = 2/3$. The observed value of $R \approx 2$ when total energy < 3 GeV is experimental evidence for the 3 distinct versions (i.e., colors) for each quark type. (The J/ψ peak marks the appearance of a fourth quark).

